Interaction of Streptavidin-Based Peptide—MHC Oligomers (Tetramers) with Cell-Surface TCRs

Jennifer D. Stone, Maxim N. Artyomov, Adam S. Chervin, Arup K. Chakraborty, Herman N. Eisen and David M. Kranz

J Immunol 2011; 187:6281-6290; Prepublished online 18 November 2011;
doi: 10.4049/jimmunol.1101734
http://www.jimmunol.org/content/187/12/6281

Supplementary Material
http://www.jimmunol.org/content/suppl/2011/11/18/jimmunol.1101734.DC1

References
This article cites 53 articles, 28 of which you can access for free at:
http://www.jimmunol.org/content/187/12/6281.full#ref-list-1

Why The JI? Submit online.
• Rapid Reviews! 30 days* from submission to initial decision
• No Triage! Every submission reviewed by practicing scientists
• Fast Publication! 4 weeks from acceptance to publication

*average

Subscription
Information about subscribing to The Journal of Immunology is online at:
http://jimmunol.org/subscription

Permissions
Submit copyright permission requests at:
http://www.aai.org/About/Publications/JI/copyright.html

Email Alerts
Receive free email-alerts when new articles cite this article. Sign up at:
http://jimmunol.org/alerts
Interaction of Streptavidin-Based Peptide–MHC Oligomers (Tetramers) with Cell-Surface TCRs

Jennifer D. Stone,*1 Maxim N. Artyomov,†‡§×1 Adam S. Chervin,*
Arup K. Chakraborty,†‡§×1 Herman N. Eisen,‖§× and David M. Kranz*2

The binding of oligomeric peptide–MHC (pMHC) complexes to cell surface TCR can be considered to approximate TCR–pMHC interactions at cell-cell interfaces. In this study, we analyzed the equilibrium binding of streptavidin-based pMHC oligomers (tetramers) and their dissociation kinetics from CD8pos T cells from 2C-TCR transgenic mice and from T cell hybridomas that expressed the 2C TCR or a high-affinity mutant (m33) of this TCR. Our results show that the tetramers did not come close to saturating cell-surface TCR (binding only 10–30% of cell-surface receptors), as is generally assumed in deriving affinity values (Kd), in part because of dissociative losses from tetramer-stained cells. Guided by a kinetic model, the oligomer dissociation rate and equilibrium constants were seen to depend not only on monovalent association and dissociation rates (koff and kon), but also on a multivalent association rate (μ) and TCR cell-surface density. Our results suggest that dissociation rates could account for the recently described surprisingly high frequency of tetramer-negative, functionally competent T cells in some T cell responses. The Journal of Immunology, 2011, 187: 6281–6290.

Because Abs and many Ags are soluble, it has been possible to study their interactions with a variety of methods under conditions that are physiological or nearly so. For TCRs and their peptide–MHC (pMHC) ligands, however, their natural state as integral membrane proteins on T cells and APCs limits the options for analyzing their interactions. Considerable insights have been gleaned from responses of T cells to pMHC displayed at various levels on other cells (target cells or APCs). The responses are informative particularly when correlated with measurements of equilibrium constants and reaction rates, but the latter are most often determined with rTCR and MHC molecules in the absence of CD8 and CD4 coreceptors. Because these coreceptors have a pronounced impact on the cellular responses, efforts have been made to study the binding of soluble pMHC complexes to TCR on intact CD8pos T cells (1). As monomers, these complexes are of limited use because they dissociate too rapidly from TCR (2, 3). However, pMHC oligomers bind more stably. Hence, they are widely used to identify T cells with cognate TCR and also, though much less widely, to determine TCR–pMHC affinities and reaction rates. The oligomeric forms include IgG dimers (4) and pentamers (ProlImmune, Oxford, U.K.), but most often, as in the current study, streptavidin (SA)-linked pMHC oligomers, called tetramers (5–7), as originally introduced by Altman et al. (8).

It has been generally accepted that the proportion of T cells that are stained by chromophore-labeled tetramers accurately measures the frequency of T cells that express the corresponding (cognate) TCRs. There are reports, however, of CD8pos T cells that respond specifically to pMHC on target cells, yet are not stained by the same pMHC as tetramers (9–12). Recently, a surprisingly high frequency of CD4pos T cells that are similarly tetramer-negative but functionally competent has been described in responses to infection by lymphocytic choriomenigitis virus and especially to a self-antigen [myelin oligodendrocyte glycoprotein (13)].

Studies have shown that the intensity of tetramer staining of T cells generally correlates with monovalent TCR–pMHC affinity and several other variables, including the density of TCR on T cells, lipid membrane organization, and differentiation status of the cells [activated versus naive T cells (12, 14–18)]. Estimates of the multivalent affinity (avidity) of cell surface TCR for tetramers are taken as the concentration of free tetramer at half-maximal binding of tetramer to cells, a determination that assumes saturation of surface TCR by bound tetramers at high free tetramer concentration. This assumption was questioned by a recent study (19), in which a panel of TCR that differed widely in affinity for the same pMHC was expressed in hybridomas that were stained with that pMHC in tetrameric form. Although the TCR levels were expressed at the same levels in all hybridomas, the maximal levels of tetramer staining varied considerably, raising the possibility that cell surface TCR were not saturated in any of the cells tested.

To evaluate this possibility, we analyzed in this study the equilibrium binding of pMHC tetramers and their dissociation kinetics from CD8pos T cells from 2C TCR transgenic mice and transduced T cell hybridomas that expressed the 2C TCR (20) or an engineered high-affinity mutant [m33 (21)] of this TCR. The analyses were based on a kinetic model of multimeric pMHC binding to cell surface TCR. The results establish that tetramers
did not come close to saturating cell-surface TCR, in part because of their dissociation when tetramer-stained cells are washed. Besides the intrinsic (monovalent) association and dissociation rates, critical determinants of tetramer dissociation are the multivalent association rate (μ) and the two-dimensional (2D) concentration (density) of cell-surface TCR. The rapidity of dissociation of tetramers from some TCR can account for the frequency of tetramer-negative, functionally competent T cells.

Materials and Methods

Peptides, Abs, and cells

SIY (SIYRYGL) and OVA (SIINEFKL) peptides were synthesized by the Macromolecular Core Facility of the Section of Research Sources, Penn State College of Medicine. Peptides were purified by reverse phase chromatography using a C-18 column, and masses were confirmed by MALDI. Peptide quantification by amino acid analysis was performed at the Molecular Structure Facility, University of California, Davis (Davis, CA). Fluorescein-labeled mAbs (F23.1, H57-597, 145-2C11, 53-6-7, and 53-5-8) and SA were purchased from BD Pharmingen (San Jose, CA). The 1B2 anti-2C TCR and B.8.24.3 anti-Kb mAbs were purified from hybridoma supernatant using protein G beads. 1B2 was labeled with FITC, and purified to remove excess FITC. For each fluorescein-labeled protein, the concentration was determined by measuring absorbance at 280 nm to yield protein absorbance and concentration.

Fluorescein-labeled SA was added stepwise to the biotinylated SIY/Kb complex made with calibrated fluorescein-labeled SA, for at least 5 min. Fluorescent beads were analyzed at the same cytometer settings as the stained cells, and measured fluorescence values were used to calculate the number of cell-bound Ab molecules or SA-oligomers. Data from dissociation experiments were fit by an equation describing a first-order exponential decay.

Quantification of cell surface-bound Abs and oligomers

Cells were stained at 4°C in the dark with saturating amounts of calibrated fluorescein-labeled Abs (determined by titration), or the indicated levels of SIY/Kb oligomer made with calibrated fluorescein-labeled SA, for at least 2 h. The cells were then washed for 8 min at 4°C in a large excess of FACS buffer, and resuspended immediately prior to analysis by flow cytometry (FACS Canto, BD Biosciences, San Jose, CA). Quantification of molecules per cell was derived from flow cytometry experiments in which specific fluorescence was analyzed in relation to calibrated fluorescein beads (Spherotech, Lake Forest, IL and Bangs Labs, Fishers, IN, Supplemental Figs. 1, 2). Fluorescent beads were analyzed at the same cytometer settings as the stained cells, and measured fluorescence values were used to convert corrected cell-bound fluorescence to numbers of cell-bound fluorescein-molecule equivalents. These latter values were used to calculate the number of cell-bound Ab molecules or SA-oligomers.

Model

To describe the behavior of SA-linked oligomers binding to and dissociating from T cells, we developed and applied a quantitative model. As the oligomers used in this study have on average three pMHC complexes per SA molecule (Fig. 1A, below), our model assumes that an SA-oligomer can bind to one, two, or three cell-surface TCR molecules; these various bound states are described as $L - T$, $L = T$, and $L = T = T$, where $L$ refers to oligomer (ligand) and $T$ to TCR. As described below (in Results) and shown in detail in Appendix A: Model Equations, a bound oligomer’s dissociation rate is determined by two factors: $k_{off}$, the intrinsic dissociation rate of the pMHC–TCR bond, as measured, for example, by SPR; and $\mu$ (a multivalent effect) with units of $s^{-1}$, which is related to the intrinsic (univalent) pMHC–TCR association rate, $k_{on}$ (with units of $M^{-1}s^{-1}$), and an effective concentration of surface T, as discussed below in Results.

At equilibrium, the oligomer association and dissociation rates are equal, as described by $k_{on}L + L_{bound} = k_{off}T_{total}$, where $k_{on}$ is on-rate for the monomeric pMHC–TCR interaction, as measured for instance by SPR, modified by the number of pMHC per SA molecule. If $\theta$ is the fraction of occupied receptors, $T_{free} = (1 - \theta)L_{total}$ and $L_{bound} = \theta L_{total}$, we can express the ratio of bound to free receptors as Eq. 5, which resembles the Scatchard equation (29–31), then follows. Detailed derivation of the equilibrium equations (including Eq. 5) can be found in Appendix A: Model Equations.

In describing these multivalent binding events, we assume that a pseudo-equilibrium between the T cell-bound states of an oligomer is reached rapidly compared with the overall association or dissociation of an oligomer from the T cell. This assumption is justified where $\mu > k_{off}$ as is the case
for the TCR–pMHC interactions described in this study (μ~10-40-fold larger than k_{off}). In addition, our interactions are in the range where dissociation data can be described by an exponential decay curve; a lack of rapid interconversion of bound states would result in a different shape to the dissociation data (32). In a range where this assumption is not valid, rapid interconversion of bound states would result in a different shape to the dissociation data (32).

FIGURE 1. MHC oligomer staining of retrovirally-transduced T cell hybridomas. A. Distribution of oligomeric species in oligomer (tetramer) preparations. Reduced, unboiled gradient SDS-PAGE gel of reaction of different molar ratios of biotinylated H2-K^b and SA. The K^b is biotinylated site specifically on the H chain concurrently with translation by biotin ligase-expressing E. coli, with a modification efficiency of ~50%. The following experiments were carried out using reagent corresponding to 16:1 MHC:SA ratio. B. Steady-state oligomer staining of T cell hybridomas with and without CD8β expression—corrected by subtracting fluorescence of 58^- cells without TCR or CD8 at the same conditions. C. Steady-state staining of 2C transgenic T cells carried out at 4°C using various concentrations of SIY/K^b:SA-oligomer. Binding of SIY/K^b:SA-oligomer to C57BL/6 T cells was subtracted from binding to 2C transgenic T cells. Quantification of molecules per cell indicates number of fluorescent SAAs associated with the cell; actual number of MHC-bound TCRs may be up to three times higher.

can be obtained from Eq. 2 in the text, the derivation of which can be found in Appendix A: Model Equations.

In this model, we also assume no positive or negative cooperativity of binding, which could affect on-rates or off-rates beyond the statistical factors we have applied to μ and k_{off}. Although this assumption may not be fully accurate, there is no clear way to account for such effects. Based on the successful application of this model to our data, we suspect that any cooperativity, if present, does not affect our overall conclusions.

**Results**

**Characterization of pMHC–SA-linked oligomers (tetramers)**

The complexes formed by SA with biotinylated MHC, usually called tetramers, vary in the number of biotinylated MHC molecules per SA molecule (33, 34). Fig. 1A shows the distribution of oligomers when biotinylated class I MHC and SA were combined at different molar ratios. Based on these results, the preparations used for subsequent work (below) were, assembled with a 16:1 molar ratio of SIY/K^b:SA; they consisted of ~40% trimer, and 20% each tetramer, dimer, and monomer bound to SA. Because of the size distribution (Fig. 1A), we refer to them subsequently as SA-oligomers, or simply oligomers, rather than as tetramers.

**Analysis of steady-state binding of pMHC oligomers to T cells**

To relate oligomer binding to TCR affinity, CD8 contribution, and cell surface levels of TCR and CD8, we first measured the steady-state binding of SIY/K^b oligomers to T cell hybridomas that expressed the 2C TCR (20) or an engineered, high-affinity mutant [m33 (21)] of this TCR (Fig. 1B), and also to naive CD8^+ 2C T cells freshly isolated from spleens of 2C TCR transgenic mice (Fig. 1C). CD8α and CD8β were coexpressed in some of the hybridomas. After the cells were incubated on ice for 2 h with oligomers at various concentrations, they were dispersed in a large volume of cold buffer, centrifuged, and the pelleted cells resuspended immediately before analysis by flow cytometry. The cell-bound oligomers increased with increasing free oligomer concentration to a maximum level and reached a plateau, or declined slightly, at the highest concentrations (Fig. 1B, 1C). The treatment used in this study is typical of oligomer staining protocols where binding is allowed to reach steady-state, and the cells are washed prior to analysis by flow cytometry. Although these data may be fit by a sigmoidal curve similar to equilibrium binding data giving a 50% maximum value (K_{D,olig}, the oligomer concentration that resulted in half-maximal binding was about the same with CD8 pos and CD8 neg T cells freshly isolated from spleens of 2C TCR. The oligomer concentration that resulted in half-maximal binding was about the same with CD8 pos and CD8 neg T cells that expressed the 2C TCR (20) or an engineered, high-affinity mutant [m33 (21)] of this TCR (Fig. 1B), and also to naive CD8^+ 2C T cells freshly isolated from spleens of 2C TCR transgenic mice (Fig. 1C). CD8α and CD8β were coexpressed in some of the hybridomas. After the cells were incubated on ice for 2 h with oligomers at various concentrations, they were dispersed in a large volume of cold buffer, centrifuged, and the pelleted cells resuspended immediately before analysis by flow cytometry. The cell-bound oligomers increased with increasing free oligomer concentration to a maximum level and reached a plateau, or declined slightly, at the highest concentrations (Fig. 1B, 1C). The treatment used in this study is typical of oligomer staining protocols where binding is allowed to reach steady-state, and the cells are washed prior to analysis by flow cytometry. Although these data may be fit by a sigmoidal curve similar to equilibrium binding data giving a 50% maximum value (K_{D,olig}, the oligomer concentration that resulted in half-maximal binding was about the same with CD8 pos and CD8 neg T cells freshly isolated from spleens of 2C TCR transgenic mice (Fig. 1C). CD8α and CD8β were coexpressed in some of the hybridomas. After the cells were incubated on ice for 2 h with oligomers at various concentrations, they were dispersed in a large volume of cold buffer, centrifuged, and the pelleted cells resuspended immediately before analysis by flow cytometry. The cell-bound oligomers increased with increasing free oligomer concentration to a maximum level and reached a plateau, or declined slightly, at the highest concentrations (Fig. 1B, 1C). The treatment used in this study is typical of oligomer staining protocols where binding is allowed to reach steady-state, and the cells are washed prior to analysis by flow cytometry. Although these data may be fit by a sigmoidal curve similar to equilibrium binding data giving a 50% maximum value (K_{D,olig}, the oligomer concentration that resulted in half-maximal binding was about the same with CD8 pos and CD8 neg T cells freshly isolated from spleens of 2C TCR transgenic mice (Fig. 1C). CD8α and CD8β were coexpressed in some of the hybridomas. After the cells were incubated on ice for 2 h with oligomers at various concentrations, they were dispersed in a large volume of cold buffer, centrifuged, and the pelleted cells resuspended immediately before analysis by flow cytometry. The cell-bound oligomers increased with increasing free oligomer concentration to a maximum level and reached a plateau, or declined slightly, at the highest concentrations (Fig. 1B, 1C). The treatment used in this study is typical of oligomer staining protocols where binding is allowed to reach steady-state, and the cells are washed prior to analysis by flow cytometry. Although these data may be fit by a sigmoidal curve similar to equilibrium binding data giving a 50% maximum value (K_{D,olig}, the oligomer concentration that resulted in half-maximal binding was about the same with CD8 pos and CD8 neg T cells freshly isolated from spleens of 2C TCR transgenic mice (Fig. 1C). CD8α and CD8β were coexpressed in some of the hybridomas. After the cells were incubated on ice for 2 h with oligomers at various concentrations, they were dispersed in a large volume of cold buffer, centrifuged, and the pelleted cells resuspended immediately before analysis by flow cytometry. The cell-bound oligomers increased with increasing free oligomer concentration to a maximum level and reached a plateau, or declined slightly, at the highest concentrations (Fig. 1B, 1C). The treatment used in this study is typical of oligomer staining protocols where binding is allowed to reach steady-state, and the cells are washed prior to analysis by flow cytometry. Although these data may be fit by a sigmoidal curve similar to equilibrium binding data giving a 50% maximum value (K_{D,olig}, the oligomer concentration that resulted in half-maximal binding was about the same with CD8 pos and CD8 neg T cells freshly isolated from spleens of 2C TCR transgenic mice (Fig. 1C). CD8α and CD8β were coex...
type 2C TCR, the half-maximal concentrations with CD8<sup>neg</sup> and CD8<sup>pos</sup> hybridomas, 2.8 nM and 4.8 nM, respectively, were surprisingly also similar (Fig. 1B); the small difference implied that the coexpressed CD8 had, if anything, a negative effect on this TCR’s affinity for pMHC. Among the questions raised by these findings is whether the SA-oligomers can engage all cell-surface TCR and measure TCR affinity for pMHC.

Do oligomers at high concentration saturate cell-surface TCRs?

To determine if saturation is approached, we measured the number of surface TCR molecules per cell, using fluorescein-labeled mAbs to various TCR domains (Cβ and Vβ8) and to the TCR-associated protein, CD3; we also used the fluorescein-labeled clonotypic Ab 1B2, which is specific for the 2C TCR (but does not bind to the 2C mutant m33). The results are shown in Fig. 2A, 2B, and summarized in Table I. As noted in the legend to Table I, the number of surface TCR molecules per cell was estimated to be twice the number of Ab molecules bound (to account for Ab binding bivalently). The number of TCR may be slightly lower, as some anti-TCR Ab molecules may be bound monovalently. Studies have shown that although the TCR complex can assemble as a monomer (36), the TCR may exist on the cell surface, at least in part, as a dimer (37–39) or oligomer (40, 41) and may preferentially bind Abs bivalently (39). It is, of course, possible that not all the TCRs measured by Ab quantification are conformationally able to bind pMHC at any given time.

As the oligomers are trimeric on average (Fig. 1A), and are thought to behave functionally as trimers, the number of TCR engaged by bound oligomers was taken to be (at most) three times the maximum number of bound oligomers in the titrations shown in Fig. 1B, 1C. From the ratio of oligomer-engaged TCR to the total number of TCR it appeared that not >10–30% of cell surface TCR was maximally engaged by bound oligomers.

Dissociation kinetics of cell-bound tetramers

One possible reason for the apparent failure to engage more cell surface TCR is that bound oligomers are lost when cells are washed prior to flow cytometry. To evaluate this possibility, we examined the dissociation of SIY/K<sup>b</sup> oligomers from oligomer-stained cells (Fig. 3A, 3B). The steps involved in dissociation can be represented by:

**FIGURE 2.** Detection of T cell receptor and CD8 epitopes on T cell hybridomas and transgenics. Quantification of molecules per cell is derived from flow cytometry staining data using calibrated, fluorescein-labeled Abs and comparing to two independent batches of fluorescein-labeled beads. A–D, Staining of cell-surface epitopes including (A, C) TCR Cβ (clone H57-597), TCR Vβ8 (clone F23.1), CD3ε (clone 145-2C11), the 2C TCR specifically (clone 1B2), and (B, D) CD8α (clone 53-6.7) and CD8β (clone 53-5.8) on (A, B) T cell hybridomas or (C, D) mouse T cells. Error bars represent the SD for at least two and up to eight repetitions for each individual measurement. E and F, Contrast images showing the size differences between (E) mouse T cells (2C TCR transgenic) and (F) T cell hybridomas (m33 TCR).
The Journal of Immunology 6285

Table I. Cell surface density of TCR and CD8 on splenic T cells and transduced T cell hybridomas

<table>
<thead>
<tr>
<th>Average No. Ab Molecules Bound per Cell (×10^3)</th>
<th>Abs to:</th>
</tr>
</thead>
<tbody>
<tr>
<td>T Cells</td>
<td>TCR Cβ⁺</td>
</tr>
<tr>
<td>CD8αβ only</td>
<td>0.2</td>
</tr>
<tr>
<td>2C TCR</td>
<td>6.8</td>
</tr>
<tr>
<td>2C TCR + CD8αβ</td>
<td>9.7</td>
</tr>
<tr>
<td>m33 TCR</td>
<td>9.3</td>
</tr>
<tr>
<td>m33 TCR + CD8αβ</td>
<td>11.0</td>
</tr>
<tr>
<td>CD8⁺ splenic T cells</td>
<td></td>
</tr>
<tr>
<td>C57BL/6</td>
<td>25.6</td>
</tr>
<tr>
<td>2C TCR transgenic</td>
<td>26.7</td>
</tr>
</tbody>
</table>

Where *L* is the amount of bound oligomer at a particular state (1), and *L* is the amount bound initially.

As seen in Fig. 3A, 3B, the dissociation rates from each of the hybridomas and T cells could indeed be fitted by a single-value exponential decay constant (*k*off), which is equivalent to *k*off *μ* / (3koff *μ*^2 + 3koffμ + μ^2) in Eq. 2. This suggests that we are in a regime where the assumption of a rapid interconversion of bound states is valid, as has been assumed previously (32).

From the experimentally determined *k*off values (Fig. 3), the amounts of oligomer lost during the ~8 min spent in washing oligomer-stained cells (see Materials and Methods) can be estimated. Correction for these losses still indicated that saturation was far from having been achieved before washing cells, especially for the freshly isolated CD8⁺ splenic T cells. These corrections were based initially on dissociation rates measured at 25°C (Fig. 3A, 3B). But, as the cells were washed in the cold (~10°C), where longer t1/2 values are expected, the actual losses were likely even smaller. To find out how much smaller, we took advantage of the intrinsic (monovalent) on- and off-rates for the binding of the SIY/K*β* complex by the 2C and m33 TCR measured by SPR at 25°C and 10°C (Ref. 19 and Table III). Based upon the following argument, these intrinsic rates could be used, together with the *k*off measured at 25°C, to estimate *k*off at 10°C.

As is discussed in Appendix A: Model Equations, the difference in dimensions of μ (measured in s⁻¹) and intrinsic monovalent on-rates, *k*on (which are measured for reactants in solution and expressed in M⁻¹s⁻¹) arises because μ already incorporates the TCR concentration in the form of the cell-surface density in the vicinity of the bound oligomer; i.e., μ = *k*off × local surface density of TCR, where *k*on is essentially the monovalent *k*on as measured by SPR (see below). On the assumption that the local and overall cell-surface TCR density for a given T cell is the same at 25°C and 10°C, it follows that

\[
\mu_{10°C} = \frac{k_{on,10°C}}{k_{on,25°C}}.
\]

Values for *k*on at the two temperatures are shown in Table III for m33 and several other engineered mutants of the 2C TCR. From these values, *k*off at 10°C can be obtained by using the relationships outlined in the mathematical model. The correction for losses during an 8 min wash at ~10°C indicate that before oligomer-stained cells were washed only ~15% of the TCR molecules on splenic CD8⁺ T cells and ~40% of those on the T cell hybridomas were engaged by the SA-oligomers at the highest oligomer concentrations tested (Fig. 1B, 1C, Table II).

The extent to which bound oligomers are lost by dissociation from stained cells varies with the decay constant (*k*off,app) and the time spent preparing cells for flow cytometry (Fig. 3C). Because *k*off and intrinsic TCR–pMHC affinity (*K*β) are correlated (Table III) (12, 16, 18, 19, 26), these losses are negligible for the engi-
neered high affinity TCR. But for lower affinity TCR, such as the 2C TCR with the Y48 or S51/Y48 mutations, ∼80–90% of bound oligomers would be lost under conditions that are commonly used to prepare oligomer-stained cells for flow cytometry.

CD8 effect on TCR–pMHC binding

From Fig. 3, it is evident that the presence of CD8αβ on the cells led to slower oligomer dissociation. For the wild-type 2C TCR on the CD8pos hybridoma, dissociation was so fast that the rate could hardly be measured. However, with CD8pos hybridoma that expressed the same TCR at about the same level, t1/2,app increased to >2 min (Fig. 3A and inset). For hybridomas that expressed the high-affinity m33 TCR, the oligomer dissociation t1/2 increased from 5.9 min on CD8pos cells to 8.5 min on CD8pos cells (Fig. 3B).

To compare T cell hybridomas with T cells freshly isolated from mice, CD8pos T cells from Rag–/– 2C TCR transgenic splenocytes were examined side-by-side with CD8pos m33 TCR+ hybridomas (Fig. 3B). Interestingly, the oligomer off-rate was nearly identical for the two cell types, despite marked differences in TCR affinities, TCR densities, and CD8 expression.

Why do oligomers dissociate more slowly from CD8pos 2C T cells than from CD8pos hybridomas that express the same TCR (t1/2,app = 5.85 and 2.1 min, respectively) (Fig. 3A, 3B)? The answer likely lies in the much greater number of TCR per cell on the cells (56,000/cell on the CD8pos T cells versus ∼25,000/cell on the CD8pos hybridomas, Fig. 2C, 2D, Table I). Moreover, the splenic CD8pos T cell diameter is about one-third that of hybridomas (Fig. 2E, 2F). These differences mean that the cell-surface TCR density is on average ∼20-fold greater on the splenic T cells than on the hybridomas (188/μm² versus 8/μm²), resulting in the larger multivalent on-rate (μ) and smaller koff (larger t1/2,app) on the T cells. This average density found on normal and transgenic T cells is consistent with what has been observed previously (42). Precise measurements of density are difficult, however, as the membranes of lymphocytes are not simple spheres (43), and local variations in TCR density are expected (reviewed in Ref. 44), which could influence binding properties. Because the intrinsic koff rate is expected to be the same from the 2C TCR, whether expressed by splenic T cells or the transduced hybridomas, the greater stability of the SA-oligomers on the splenic T cells can be attributed to the faster on-rate (μ) on the T cells.

Oligomer equilibrium binding constants (K_D,olig)

Although cell-bound pMHC oligomers do not saturate cognate cell-surface TCR, the titration curves in Fig. 1B, 1C indicate that they saturate a subset of these TCR (19). For this subset, the processes that occur on oligomer binding at steady state can be represented as:

\[ L_{sol} + T \xrightarrow{\text{on}} k_{on} T \xrightarrow{\text{off}} L + T \xrightarrow{2k_{off}} L \]

where all of the terms are defined as in Eq. 1 except for k’_off, which refers to the on-rate for the first pMHC of the oligomer to bind. We take k’_off to be the monomeric pMHC–TCR on-rate (measured for example by SPR), except for a statistical factor that takes into account the number of pMHC per oligomer (three in the present case). The binding data can be treated according to the Langmuir adsorption isotherm to obtain an expression for the fraction of cell-surface sites (i.e., TCR) occupied by the pMHC oligomers as a function of the free oligomer concentration. Accordingly,

\[ \frac{\theta}{1-\theta} = \frac{k_{on} L_{sol} (3k_{off}^2 + 3k_{off}(\mu + \mu^2))}{k_{off}^3} = k_{on} L_{sol} \frac{L_{sol}}{k_{off}} \]

where L_{sol} is the concentration of oligomers in solution, and θ is the fraction of sites occupied by oligomers (singly, doubly, or triply bound). In deriving Eq. 5 (see Appendix A: Model Equations), we have assumed that the concentration of oligomers in solution is essentially equal to the initial oligomer concentration and that this approximation is valid when the latter quantity is relatively large.

FIGURE 3. MHC oligomer dissociation from T cells. A and B. Remaining associated fluorescent pMHC oligomer measurements were made for (A) 2C hybridomas with (open triangles) or without (closed circles) CD8 (highlighted in inset), and m33 with (open squares) or without (closed diamonds) CD8. B. 2C TCR transgenic T cells (closed circles) and m33 hybridomas (CD8−, open diamonds). Dissociation data for A and B were fit by the equation describing a first-order exponential decay. C. Simulated effect of dissociation of bound oligomers on washing the cells over a 4, 8, or 12 min period in the cold (4°C). Simulated effect of dissociation of bound oligomers on washing the cells over a 4, 8, or 12 min period in the cold (4°C–10°C) prior to flow cytometry, showing the effect of koff,app on the level of persisting oligomers. Vertical bars indicate approximate koff,app values calculated for different 2C receptor mutants.
From the titration shown in Fig. 1C, the apparent affinity (K_{D,olig}) of the 2C TCR on splenic CD8\textsuperscript{pos} T cells for SA-SIY/K\textsuperscript{b} oligomers is \sim 1 nM, as determined by the free oligomer concentration at 50% maximum bound. Comparisons of K_{D,olig} to monovalent K\textsubscript{D} are useful to demonstrate the benefits of multivalent ligand binding to TCR (e.g., the K\textsubscript{D}/K_{D,olig} ratio has been termed an enhancement factor) (19, 45).

**Discussion**

This study confirms previous indications that SA-based pMHC oligomers (tetramers) bind stably to only a fraction of cognate cell surface TCR (19). The fraction amounted to \sim 15% of the TCR on CD8\textsuperscript{pos} splenic T cells from 2C TCR transgenic mice and \sim 40% on a TCR-transduced hybridoma line. These less-saturating levels arise in part from losses of bound oligomers when oligomer-stained cells are washed. The extent of these losses depends on the dissociation or decay constant, k\textsubscript{off,olig}, which is related to TCR–pMHC affinity (Fig. 3C and Eq. 2). For T cells for which TCR binds oligomers weakly (large k\textsubscript{off}), nearly all bound oligomers may be lost by dissociation when cells are subjected to commonplace washing conditions. This effect could account for reports of tetramer-negative functionally competent CD8\textsuperscript{pos} T cells (9–12). Losses of bound oligomers by dissociation from low-affinity TCR may also well account for the recent report of a surprisingly high frequency of CD4\textsuperscript{pos} T cells that respond specifically to pMHC but are not stained by the corresponding tetramers (13). The frequency of such tetramer-negative, functionally competent T cells would be expected to be higher in CD4\textsuperscript{pos} than in CD8\textsuperscript{pos} T cell populations because of differences in their coreceptor ectodomain binding to MHC; CD8 generally binds weakly to class I MHC but CD4 binds hardly at all to class II MHC (46, 47).

It is likely that the oligomers bind stably (multivalently) only to those TCR molecules that are closely clustered. The spacing between biotin (pMHC) binding sites on SA is 2–4 nm (48), whereas TCR, if uniformly distributed on the cell surface, would generally be much further apart (separated on average by \sim 60–70 nm on a T cell of 8.5 \mu m diameter with 56,000 TCR molecules per cell [Fig 2E, Table I]). But cell-surface TCR, like many other integral membrane proteins, are aggregated into groups (“islands”), some depending upon cholesterol (lipid rafts) for their clustering (15, 49–51; reviewed in Ref. 52). Whether the SA-oligomers bind selectively to particular TCR clusters is not clear. The stronger binding of pMHC dimers to activated than to naive T cells and abolition of this difference by reducing cholesterol content of the cell membranes (15) indicate that oligomer binding has the potential to be developed into a useful procedure to define the size and character of TCR clusters on cells that differ functionally or in developmental status.

For the TCR subset that can stably engage SA-oligomers, an apparent equilibrium constant for the oligomer–TCR interaction (K_{D,olig}) can be defined as the free SA-oligomer concentration that

<table>
<thead>
<tr>
<th>TCR hybridsomas expressing</th>
<th>Total No. TCR per cell</th>
<th>Maximum No. TCR Engaged by pMHC Oligomers</th>
<th>Measured 25°C</th>
<th>10°C</th>
</tr>
</thead>
<tbody>
<tr>
<td>2C TCR</td>
<td>15,300</td>
<td>2985</td>
<td>0.20</td>
<td>—</td>
</tr>
<tr>
<td>2C TCR and CD8αβ</td>
<td>19,700</td>
<td>2058</td>
<td>0.10</td>
<td>0.22</td>
</tr>
<tr>
<td>m33 TCR</td>
<td>21,700</td>
<td>6225</td>
<td>0.29</td>
<td>0.73</td>
</tr>
<tr>
<td>m33 TCR and CD8αβ</td>
<td>25,500</td>
<td>6309</td>
<td>0.25</td>
<td>0.30</td>
</tr>
<tr>
<td>CD8\textsuperscript{+} splenic T cells</td>
<td>58,200</td>
<td>(450)</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>C57BL/6</td>
<td>56,400</td>
<td>7050</td>
<td>0.13</td>
<td>0.32</td>
</tr>
</tbody>
</table>

\*From Table I.
\*Maximum level of MHC oligomer saturation measured, allowing for three MHC engaged per SA-oligomer.
\*Maximum TCR occupancy estimated at steady-state correcting for losses during a preanalysis wash carried out at 25°C.
\*Maximum TCR occupancy estimated at steady-state correcting for losses during a preanalysis wash carried out at 10°C.
\*Conversion of k\textsubscript{off,olig} for 2C uses k\textsubscript{off} and k\textsubscript{on} for 2C measured at 25°C, but k\textsubscript{off} and k\textsubscript{on} for the closely-related TCR Y48 measured at 10°C (Table III).

**Table III.** Binding of SIY/K\textsuperscript{b} monomer by various TCR measured by SPR at different temperatures

<table>
<thead>
<tr>
<th>TCR</th>
<th>k\textsubscript{on} (M\textsuperscript{-1}s\textsuperscript{-1})</th>
<th>k\textsubscript{off} (s\textsuperscript{-1})</th>
<th>K\textsubscript{D} (nM)</th>
<th>k\textsubscript{eff,olig} (min\textsuperscript{-1})</th>
</tr>
</thead>
<tbody>
<tr>
<td>m33</td>
<td>2.5 \times 10\textsuperscript{5}</td>
<td>0.0036</td>
<td>17.1</td>
<td>0.008</td>
</tr>
<tr>
<td>S51</td>
<td>3.5 \times 10\textsuperscript{5}</td>
<td>0.0013</td>
<td>3.97</td>
<td>0.001</td>
</tr>
<tr>
<td>Y26</td>
<td>3.3 \times 10\textsuperscript{5}</td>
<td>0.0023</td>
<td>7.2</td>
<td>0.004</td>
</tr>
<tr>
<td>Y49</td>
<td>2.3 \times 10\textsuperscript{5}</td>
<td>0.0019</td>
<td>8.6</td>
<td>0.001</td>
</tr>
<tr>
<td>N27</td>
<td>2.8 \times 10\textsuperscript{5}</td>
<td>0.0036</td>
<td>12.7</td>
<td>0.004</td>
</tr>
<tr>
<td>S51/Y48</td>
<td>1.7 \times 10\textsuperscript{5}</td>
<td>0.051</td>
<td>305</td>
<td>0.29</td>
</tr>
<tr>
<td>Y48</td>
<td>1.65 \times 10\textsuperscript{5}</td>
<td>0.185</td>
<td>1130</td>
<td>0.12</td>
</tr>
</tbody>
</table>

\textsuperscript{a}Values of monovalent binding properties carried out at 10°C by SPR.
\textsuperscript{b}Values of monovalent binding properties carried out at 25°C by SPR.
\textsuperscript{c}Values of k\textsubscript{eff,olig} at 10°C estimated from monovalent binding properties and from k\textsubscript{eff,olig} values at 25°C, using Eq. (2) and the relationship: k\textsubscript{eff,olig} = \mu \textsubscript{TCR} \times k\textsubscript{off,olig} / k\textsubscript{off,olig} \times k\textsubscript{on} at 25°C.

\textsuperscript{12}This study confirms previous indications that SA-based pMHC oligomers (tetramers) bind stably to only a fraction of cognate cell surface TCR (19). The fraction amounted to \sim 15% of the TCR on CD8\textsuperscript{pos} splenic T cells from 2C TCR transgenic mice and \sim 40% on a TCR-transduced hybridoma line. These less-saturating levels arise in part from losses of bound oligomers when oligomer-stained cells are washed. The extent of these losses depends on the dissociation or decay constant, k\textsubscript{off,olig}, which is related to TCR–pMHC affinity (Fig. 3C and Eq. 2). For T cells for which TCR binds oligomers weakly (large k\textsubscript{off}), nearly all bound oligomers may be lost by dissociation when cells are subjected to commonplace washing conditions. This effect could account for reports of tetramer-negative functionally competent CD8\textsuperscript{pos} T cells (9–12). Losses of bound oligomers by dissociation from low-affinity TCR may also well account for the recent report of a surprisingly high frequency of CD4\textsuperscript{pos} T cells that respond specifically to pMHC but are not stained by the corresponding tetramers (13). The frequency of such tetramer-negative, functionally competent T cells would be expected to be higher in CD4\textsuperscript{pos} than in CD8\textsuperscript{pos} T cell populations because of differences in their coreceptor ectodomain binding to MHC; CD8 generally binds weakly to class I MHC but CD4 binds hardly at all to class II MHC (46, 47).

It is likely that the oligomers bind stably (multivalently) only to those TCR molecules that are closely clustered. The spacing between biotin (pMHC) binding sites on SA is 2–4 nm (48), whereas TCR, if uniformly distributed on the cell surface, would generally be much further apart (separated on average by \sim 60–70 nm on a T cell of 8.5 \mu m diameter with 56,000 TCR molecules per cell [Fig 2E, Table I]). But cell-surface TCR, like many other integral membrane proteins, are aggregated into groups (“islands”), some depending upon cholesterol (lipid rafts) for their clustering (15, 49–51; reviewed in Ref. 52). Whether the SA-oligomers bind selectively to particular TCR clusters is not clear. The stronger binding of pMHC dimers to activated than to naive T cells and abolition of this difference by reducing cholesterol content of the cell membranes (15) indicate that oligomer binding has the potential to be developed into a useful procedure to define the size and character of TCR clusters on cells that differ functionally or in developmental status.

For the TCR subset that can stably engage SA-oligomers, an apparent equilibrium constant for the oligomer–TCR interaction (K_{D,olig}) can be defined as the free SA-oligomer concentration that...
CD8 effect can be increased up to 8-fold because most. For SA-linked oligomers, which are effectively trimeric, the lifetime of the TCR–pMHC bond only modestly, 2-fold at
ings (32) and computational analysis (46) concur in showing that in the trimolecular CD8–pMHC–TCR reaction. Experimental find-
the same interactions under three-dimensional conditions (2, 3).
ceptionally fast and their apparent affinities much higher than for
studies have reported the kinetics of such 2D interactions to be ex-
at the interface of T cells and target cells or other APCs. Recent
imates more closely than the other conditions in Table IV to the
TCR (41), they and nonclustered TCR have the same intrinsic
stably (multivalently) constitute a small fraction of all cell surface
the presumably clustered TCR molecules that bind SA-oligomers
and CD8 pos splenic T cells that express the same TCR (2C) (
[45x113]the lower affinity 2C TCR, 
for many rTCR and pMHC pairs) to a 300-fold higher affinity
the binding of soluble SIY/Kb complex under different conditions. The values range
from ∼30 μM (in the micromolar range commonly found by SPR
from relatively low-affinity TCR (Fig. 3
C).
ly greater difference, 50-fold, between the CD8 neg hybridoma
hybridomas that expressed the high-affinity TCR (m33) is con-
for many rTCR and pMHC pairs) to a 300-fold higher affinity for
of eight and reflects the greater dissociative losses of bound
of the
a

Table IV. Equilibrium constants (K0) for 2C TCR binding the SIY/Kb (pMHC) complex measured under various conditions

<table>
<thead>
<tr>
<th>Assay Conditions</th>
<th>K0 (μM)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Soluble, recombinant 2C TCR and SIY/Kb</td>
<td>32</td>
<td>23</td>
</tr>
<tr>
<td>SPR</td>
<td>27</td>
<td>24</td>
</tr>
<tr>
<td>Soluble monomeric SIY/Kb</td>
<td>0.1</td>
<td>54</td>
</tr>
<tr>
<td>Inhibition of [125I]-Fab 1B2 binding to CD8+ T cells</td>
<td>0.33</td>
<td>53</td>
</tr>
<tr>
<td>Dimeric SIY/Kb-IgG binding to Naive 2C transgenic T cells</td>
<td>0.004 (4°C)</td>
<td>15</td>
</tr>
<tr>
<td>Activated 2C transgenic T cells</td>
<td>0.077 (37°C)</td>
<td>15</td>
</tr>
<tr>
<td>Streptavidin-oligomers of SIY/Kb binding to CD8+ 2C cell hybridomas</td>
<td>0.011</td>
<td>19</td>
</tr>
<tr>
<td>CD8+ 2C T cell hybridomas</td>
<td>0.0041 a</td>
<td></td>
</tr>
<tr>
<td>CD8+ m33 T cell hybridomas</td>
<td>0.0023 a</td>
<td></td>
</tr>
<tr>
<td>CD8+ m33 T cell hybridomas</td>
<td>0.0010 a</td>
<td></td>
</tr>
<tr>
<td>CD8+ 2C transgenic splenic T cells</td>
<td>0.0016 a</td>
<td></td>
</tr>
</tbody>
</table>

Measurements at 25°C unless otherwise indicated.
*Values measured in current work.
leads to half-saturation of that TCR subset (Eq. 5), the main uncertainty being the maximum level. From the titration shown in Fig. 1C, K0,olig is ∼1 nM for the 2C TCR–SIY/Kb oligomer interaction on CD8pos T cells. This value is compared in Table IV with others measured for the same TCR (2C) and the same Ag (SIY/Kb complex) under different conditions. The values range from ∼30 μM (in the micromolar range commonly found by SPR for many rTCR and pMHC pairs) to a 300-fold higher affinity for the binding of soluble SIY/Kb monomer to the 2C TCR and CD8 on intact CD8pos T cells and the much higher values found with Ig-based dimers and SA-oligomers on CD8pos T cells. Although the presumably clustered TCR molecules that bind SA-oligomers stably (multivalently) constitute a small fraction of all cell surface TCR (41), they and nonclustered TCR have the same intrinsic (monovalent) affinity. This uniformity is indicated by the linearity of Scatchard plots (1, 15) and by the Sips distribution (53).

The binding of pMHC oligomers to cell-surface TCR approximates more closely than the other conditions in Table IV to the quasi 2D interactions that occur under physiological conditions at the interface of T cells and target cells or other APCs. Recent studies have reported the kinetics of such 2D interactions to be exceptionally fast and their apparent affinities much higher than for the same interactions under three-dimensional conditions (2, 3).

Finally, it is worth commenting on the contribution of CD8αβ in the trimolecular CD8–pMHC–TCR reaction. Experimental findings (32) and computational analysis (46) concur in showing that the CD8 ectodomain’s binding to the MHC α3 domain increases the lifetime of the TCR–pMHC bond only modestly, 2-fold at most. For SA-linked oligomers, which are effectively trimeric, the CD8 effect can be increased up to 8-fold because k′off is proportional to (koff)3 (Eq. 2 and Refs. 32, 46). The CD8 effect on hybridomas that expressed the high-affinity TCR (m33) is consistent with these values: t1/2 is ∼1.4-fold greater for the CD8pos than CD8neg cells (Fig. 3A). However, for hybridomas that express the lower affinity 2C TCR, t1/2 is 20-fold greater for the CD8pos than the CD8neg cells, which exceeds the estimated upper limit of eight and reflects the greater dissociative losses of bound oligomers from relatively low-affinity TCR (Fig. 3C). The still far greater difference, ∼50-fold, between the CD8pos hybridoma and CD8neg splenic T cells that express the same TCR (2C) (t1/2 ∼0.1 min versus 5.85 min), likely arises from the additional effect of the ∼20-fold greater surface density of the TCR on the splenic T cells, resulting in an increase in the multivalent on-rate (μ) and from the proportionality of k′off to koff/μ3 (Eq. 2).

Appendix A: Model Equations

**Dissociation of bound oligomers**

\[ L \equiv T \underset{k_{off}}{\xrightarrow{3k_{off}}} L + T \stackrel{2k_{off}}{\xrightarrow{2\mu}} L - T \underset{k_{off}}{\xrightarrow{3}} L_{sol}, \quad (\text{Scheme 1}) \]

where T refers to available TCR sites on the cell surface, L = T is the number of oligomers bound by three pMHC complexes, L = T is the number bound by two pMHCs, and L-T is the number bound by one pMHC, dissociation of L-T loses oligomers into solution (Lsol).

We assume that for each pMHC–TCR interaction, koff and μ (the multivalent on rate, see text) are independent of the binding of neighboring MHC with TCR. Thus, stoichiometric coefficients in front of koff and μ correspond to the number of pMHCs available for binding/unbinding.

The following differential equations were used to describe interconversion among bound forms and loss of bound forms in accord with Scheme (1):

\[ \frac{d[L - T]}{dt} = -k_{off}[L - T] + 2k_{off}[L = T] - 2\mu[L - T], \quad (A1) \]

\[ \frac{d[L = T]}{dt} = -2k_{off}[L = T] - \mu[L = T] + 2\mu[L - T] + 3k_{off}[L = T], \quad (A2) \]

and

\[ \frac{d[L = T]}{dt} = -3k_{off}[L = T] + \mu[L = T]. \quad (A3) \]

**Derivation of text Eq. 2 and 5**

**Text Eq. 2.** Concentration of oligomers (L) bound to cell-surface TCR (T) is equal to the sum of all bound forms:

\[ L_B = L - T + L = T + L = T. \quad (A4) \]
Loss of bound oligomers is determined by dissociation of the singly bound form:

\[
\frac{dL_B}{dt} = -k_{d,ff}L_B = -k_{d,ff}[L - T]. \tag{A5}
\]

As our oligomer dissociation data exhibit exponential decay kinetics, we can safely assume a rapid equilibrium and interconvertibility (mass equilibrium) of bound forms, as has been assumed previously (32). Applying this assumption, we get:

\[
[L = T] = \frac{\mu}{k_{d,ff}}[L - T], \tag{A6}
\]

\[
[L = T] = \frac{\mu}{3k_{d,ff}}[L - T] = \frac{\mu^2}{3k_{d,ff}^2}[L - T]. \tag{A7}
\]

Plugging in (A6-7) to (A4):

\[
L_B = [L - T]\left(1 + \frac{\mu}{k_{d,ff}} + \frac{\mu^2}{3k_{d,ff}^2}\right) = [L - T]\left(3\frac{k_{d,ff}^2 + \mu k_{d,ff} + \mu^2}{k_{d,ff}^2}\right). \tag{A8}
\]

Plugging (A8) in to (A5) yields Text Eq. 2:

\[
\frac{L_{bound}}{L_{bound,0}} = \exp\left[\frac{k_{d,ff}^2}{3k_{d,ff}^2 + \mu k_{d,ff} + \mu^2}\right] \approx \exp\left[\frac{-k_{d,ff}^2}{\mu^2}\right],
\]

where the approximate equality can be applied under the conditions where \(\mu \gg k_{d,ff}\), as is true for all of the interactions described in this study. Where \(\mu \leq k_{d,ff}\), the roots of the quadratic equation for \(\mu\) can be solved.

**Derivation of Text Eq. 5**

At equilibrium, the rate of oligomer association is equal to the rate of oligomer dissociation:

\[
k_{on,T_{free}} = k_{d,ff}L_{bound}.
\]

where \(k'_{on}\) is on-rate (\(k_{on}\)) for the monomeric pMHC–TCR interaction, as measured by instance by SPR, modified by the number of pMHC per streptavidin molecule.

If \(\theta\) is taken to be the fraction of occupied receptors, \(T_{free} = (1 - \theta)T_{total}\) and \(L_{bound} = \theta T_{total}\). Eq. 5 from the main text then follows:

\[
\theta = \frac{k_{on,T_{free}}L_{bound}(3k_{d,ff}^2 + \mu k_{d,ff} + \mu^2)}{k_{off}} = \frac{k_{on,L_{bound}}}{k_{d,ff}}.
\]

Eq. 5 resembles the Scatchard equation. That equation, arguably the most widely used one in immunology, was originally developed (30) to account for the equilibrium binding of small molecules and ions to proteins. For ligand–protein interactions, it is usually expressed as \(r/n = r - r = K_c\), where \(r\) represents moles bound ligand, \(n\) the moles of ligand maximally bound, \(c\) the free ligand concentration, and \(K\) the equilibrium (association) constant. Independent derivations of Scatchard’s equation have generally been based upon the distribution of bound and free ligands at equilibrium (29, 31). In contrast, Eq. 5 above was derived from the kinetics of multivalent ligand binding to cell surface receptors. If, however, Eq. 5 were applied to monovalent ligand–receptor interactions, \(\mu\) would become zero, \(K_{on}\) would correspond to the intrinsic association rate, \(k_{d,ff}\), and Eq. 5 would then be equivalent to the Scatchard equation.

**Acknowledgments**

We thank the staff of the University of Illinois Carver Biotechnology Center for assistance with flow cytometry and SPR studies.

**Disclosures**

The authors have no financial conflicts of interest.

**References**


