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Multiscale Computational Modeling Reveals a Critical Role for TNF-\(\alpha\) Receptor 1 Dynamics in Tuberculosis Granuloma Formation

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Denise E. Kirschner,† and Jennifer J. Linderman*

Multiple immune factors control host responses to *Mycobacterium tuberculosis* infection, including the formation of granulomas, which are aggregates of immune cells whose function may reflect success or failure of the host to contain infection. One such factor is TNF-\(\alpha\). TNF-\(\alpha\) has been experimentally characterized to have the following activities in *M. tuberculosis* infection: macrophage activation, apoptosis, and chemokine and cytokine production. Availability of TNF-\(\alpha\) within a granuloma has been proposed to play a critical role in immunity to *M. tuberculosis*. However, in vivo measurement of a TNF-\(\alpha\) concentration gradient and activities within a granuloma are not experimentally feasible. Further, processes that control TNF-\(\alpha\) concentration and activities in a granuloma remain unknown. We developed a multiscale computational model that includes molecular, cellular, and tissue scale events that occur during granuloma formation and maintenance in lung. We use our model to identify processes that regulate TNF-\(\alpha\) concentration and cellular behaviors and thus influence the outcome of infection within a granuloma. Our model predicts that TNF-\(\alpha\)R1 internalization kinetics play a critical role in infection control within a granuloma, controlling whether there is clearance of bacteria, excessive inflammation, containment of bacteria within a stable granuloma, or uncontrolled growth of bacteria. Our results suggest that there is an interplay between TNF-\(\alpha\) and bacterial levels in a granuloma that is controlled by the combined effects of both molecular and cellular scale processes. Finally, our model elucidates processes involved in immunity to *M. tuberculosis* that may be new targets for therapy. The Journal of Immunology, 2011, 186: 3472–3483.

The key pathological feature of TB that arises as a result of the immune response is the formation of aggregates of bacteria and immune cells within the lung called granulomas. TB granulomas, especially in humans, form as organized spherical structures composed of bacteria, a macrophage-rich core including resting, infected, and activated macrophages, and a surrounding mantle of lymphocytes. Granulomas act to immunologically restrain and physically contain *M. tuberculosis* infection (4–10). Latent and active TB in humans comprise a heterogeneous mixture of granulomas in both lung and lymph nodes that provide a range of physiological microenvironments associated with bacterial replication, persistence, and killing. Characterization of different types of granulomas will provide a framework for understanding of the immunobiology of TB that can lead to the development of new strategies for control and therapy (11, 12).

In addition to cellular components, studies in animal models and humans have identified a variety of cytokines involved in granuloma formation and function, including TNF-\(\alpha\) and IFN-\(\gamma\) (reviewed in Ref. 13). These molecules are secreted from cellular sources (macrophages and T cells) as a result of *M. tuberculosis* infection, interact with receptors on target cells, trigger intracellular signaling pathways, and induce cell responses that ultimately contribute to formation of granulomas and immunologic control of *M. tuberculosis* infection (13–15). One can hypothesize that molecular scale processes that lie between the availability of particular extracellular cytokines and the final cytokine-mediated response may influence the outcome of *M. tuberculosis* infection. Receptor–ligand binding and trafficking (defined in this article to include synthesis, internalization, recycling, and degradation of the ligand and receptors) represent a group of molecular scale processes that take place under physiological conditions and are believed to play a major role in receptor-mediated cell responses (16). However, the significance of trafficking processes in controlling the
effect of cytokines on the host immune response (TB immune response in particular) has never been studied. Hence, a multiscale approach that considers events at the molecular, cellular, and tissue scales is required for comprehensive analysis of the role of cytokines in the complex immune response to *M. tuberculosis*.

Our study is focused on TNF-α interactions with immune cells that form a granuloma. The pleiotropic cytokine TNF-α is produced by a variety of immune cells, especially infected and activated macrophages and proinflammatory T cells (17, 18), and functions as part of the immune response to *M. tuberculosis* infection via several mechanisms. TNF-α (in conjunction with the cytokine IFN-γ) induces macrophage activation (19–21), enhances immune cell recruitment to the site of infection (22), and augments chemokine expression by macrophages through activation of the NF-κB signaling pathway (23). TNF-α can also mediate cell death via inducing the caspase-mediated apoptotic pathway (24, 25). Data identifying the roles of TNF-α include TNF-α knockout/neutralization experiments in mice and monkeys (17, 26–28), TNF-αR1 (TNFR1) knockout experiments in mice (17), and mathematical modeling studies (29, 30). Despite this wealth of information on the critical role of TNF-α in immunity to *M. tuberculosis*, many fundamental questions remain unanswered regarding the mechanisms that regulate TNF-α activity at different biological scales. For example, it is not known how the dynamics of molecular events such as TNF-α–TNFR binding and trafficking influence a granuloma’s ability to control *M. tuberculosis* infection. We have recently suggested via mathematical modeling that organization of immune cells as well as the processes of TNF-α–TNFR binding and trafficking control steady-state TNF-α availability within an existing granuloma. This results from a TNF-α concentration gradient that is created with the highest concentration at the core of granuloma (31). However, important unanswered questions remain: What factors control such a gradient during a long-term immune response to *M. tuberculosis* infection that includes formation and maintenance of granulomas? How does this gradient regulate TNF-α–associated processes and ultimately translate to the outcome of *M. tuberculosis* infection? Is there an interplay between TNF-α availability and bacterial load in a granuloma? Are there TNF-α–level processes that, if targeted, could present new strategies for disease therapy?

These questions invoke multiple biological scales (in length and time) that are currently difficult to address experimentally. Hence, a systems biology approach that incorporates computational modeling to generate and test hypotheses, run virtual experiments, and make experimentally testable predictions is uniquely suited to address these questions. We develop a multiscale computational model that describes the immune response to *M. tuberculosis* in the lung over three biological length scales: molecular, cellular, and tissue. We use the model to track formation and maintenance of a granuloma in space and time. The model captures the dynamics of TNF-α–TNFR interactions that occur on the second to minute timescales within the long-term immune response to *M. tuberculosis* infection, a complex process that lasts for months to years. We identify TNF-α–associated processes that influence infection outcome at the granuloma scale as well as predict cellular scale processes that influence TNF-α availability. Finally, we identify processes that regulate TNF-α concentration and cellular behaviors and thus influence the outcome of infection within a granuloma.

**Materials and Methods**

An overview of the multiscale granuloma model

To build a multiscale model necessary to address the questions regarding TNF-α–regulated immune responses to *M. tuberculosis* infection in the lung, we need to first have working models at both the cellular/tissue scale and the molecular/single-cell scale. We briefly describe these models below and then describe our approach for linking them. Cellular and tissue scale dynamics are captured via a set of well-described interactions between immune cells and *M. tuberculosis* at the site of infection using stochastic simulations in the form of an agent-based model (ABM). Single-cell molecular scale processes that control TNF-α–TNFR binding and trafficking for each individual cell are captured by a set of nonlinear ordinary differential equations (ODEs). Fig. 1 indicates how these models exist separately and how they are linked into a single multiscale granuloma model. The linkage is achieved via TNF-α–induced cell responses (i.e., apoptosis and NF-κB activation) that are modeled as Poisson processes with rate parameters computed as functions of molecular concentrations from the ODE model. Further details of the rules, equations, and parameters of the multiscale model are described in this article and in the online supporting text, tables, and videos at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/.

**Cellular/tissue scale model**

The two-dimensional (2-D) ABM used in this study is an updated version of our previous model that captures cellular scale interactions leading to a tissue-level readout, namely granuloma formation in response to *M. tuberculosis* infection (32). Fig. 1A depicts a schematic overview of selected immunological interactions tracked at the cellular scale. A full description of all ABM rules that reflect known biological activities is provided in the online supporting text at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/ and significant updates to the original model are highlighted. Briefly, rule events include chemotactic movement and recruitment of immune cells to site of infection, intracellular and extracellular growth of *M. tuberculosis*, phagocytosis of bacteria by macrophages, cell death and apoptosis, macrophage–T cell interactions such as cytokolytic functions of cytotoxic T cells and IFN-γ based activation of macrophages by proinflammatory T cells (Ty), downregulation of immune cells by regulatory T cells, secretion of chemokines, and caseation.

One important simplification in our model is the choice to include only cell types with well-characterized roles in *M. tuberculosis* granulomas (macrophages, cytotoxic T cells, Ty, and T regulatory cells). Cell types that may have important roles but are not sufficiently characterized at this point to include in mechanistic ways in the model include neutrophils (with protective roles in early infection that may be immunomodulatory in nature (33–35), multinucleate giant cells [may modulate chemokine production (36, 37)], dendritic cells [for optimal antigen stimulation of T cells (38, 39), and foamy cells [possible nutrient source for bacteria (40, 41)]. Future work can easily incorporate them into the model when more mechanistic data become available.

**Molecular/single-cell scale TNF-α–TNFR model**

The kinetic processes of TNF-α–TNFR binding and trafficking (synthesis, internalization, recycling, and degradation of ligand and receptors) occurring in individual cells within a granuloma can be described by ODEs (31). As schematically shown in Fig. 1B, TNF-α is first synthesized by TNF-α–producing cells, including infected macrophages, chronically infected macrophages, NF-κB–activated resting macrophages, activated macrophages and T cells, as a membrane-bound precursor form (mTNF) that can then be processed and released as a soluble form (sTNF) into extracellular spaces. Two types of TNFR (TNFR1 and TNFR2) are synthesized and expressed on the cell membrane. The equations describing the kinetic processes of TNF-α–TNFR binding and trafficking for each individual cell are captured by a set of nonlinear or differential equations in the online supporting text and Tables S3 and S4 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/.

**Linking the individual models via sTNF-induced cell responses**

Activation of the two major TNF-α–induced signaling pathways, the caspase-mediated apoptotic pathway and the NF-κB pathway, are both controlled at the level of sTNF–TNFR1 interactions and thus serve as the link between the molecular/single-cell scale TNF-α–TNFR kinetic model and the cellular/tissue scale model. The NF-κB signaling pathway is initiated by sTNF-bound cell surface TNFR1, and apoptosis depends on the internalized sTNF–TNFR1 complexes (42–44). As described in the literature, NF-κB activation of macrophages is a necessary but not sufficient factor in successful immune response to mycobacterial infection. Its role
includes induction of a variety of inflammatory-related genes such as TNF-α and chemokines as well as controlling phagolysosome fusion-mediated killing of mycobacteria by activated macrophages (20, 45). TNF-α–induced apoptosis of macrophages kills intracellular bacteria and is associated with a better outcome of infection (3). In addition to sTNF, mTNF has also been shown to contribute in part to control of M. tuberculosis infection in mice (46–48). However, experimental data regarding molecular and cellular-level details of mTNF-mediated signaling and reverse signaling in M. tuberculosis immune responses are limited. Thus, at this time we only consider in our model signaling mediated by sTNF–TNFR1.

A recent study has shown that TNF-α–induced NF-κB activation is a process with a discrete nature at the single-cell level, with fewer cells responding at lower doses (49). Accordingly, we describe TNF-α–induced NF-κB activation for each individual macrophage as a Poisson process with a probability determined within each time-step (Δt), based on a Poisson rate parameter that is a function of the NF-κB activation constant (κB,ab), the concentration of cell surface sTNF–TNFR1 complex [sTNF–TNFR1], and the concentration threshold for cell surface sTNF–TNFR1 (fTNFR1):

\[
P_{\text{apopt}}(t) = \begin{cases} 0 & \text{[sTNF–TNFR1]} < k_{\text{apopt}} \\ 1 - e^{-k_{\text{apopt}}[\text{[sTNF–TNFR1]}]} & \text{[sTNF–TNFR1]} \geq k_{\text{apopt}} \end{cases}
\]

(1)

Similarly, we model TNF-α–induced apoptosis for each individual cell (macrophage and T cell) by:

\[
P_{\text{apopt}}(t) = \begin{cases} 0 & \text{[sTNF–TNFR1]} < k_{\text{apopt}} \\ 1 - e^{-k_{\text{apopt}}[\text{[sTNF–TNFR1]}]} & \text{[sTNF–TNFR1]} \geq k_{\text{apopt}} \end{cases}
\]

(2)

We use a Poisson process with a probability computed as a function of the apoptosis rate constant (κapopt), the concentration of internalized sTNF–TNFR1 complexes [sTNF–TNFR1], and the concentration threshold for internalized sTNF–TNFR1 (fTNFR1). Scale-linking parameters, or simply “linking parameters”, that is, TNF-α–response parameters (defined to include parameters introduced in Equations 1 and 2), are listed in Table S5 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/.

To analyze how TNF-α affects infected versus resting macrophages in a granuloma, we define infected/resting cell ratios, R_{\text{apopt}} and R_{\text{apopt}}, as follows. R_{\text{apopt}} is defined as the ratio of the number of infected macrophages that undergo TNF-α–mediated apoptosis to the number of resting macrophages that undergo TNF-α–mediated apoptosis during a 200-d period postinfection. R_{\text{apopt}} is similarly defined as the number of infected macrophages that undergo TNF-α–mediated NF-κB activation to the number of resting macrophages that undergo TNF-α–mediated NF-κB activation during a 200-d period postinfection.

Parameter estimation and control experiments

We estimate ABM parameter values from literature data as described in detail by Ray et al. (30). When data are not available, we use uncertainty analysis to explore the entire parameter space of possible model outcomes as described in Ref. 50. Cell-specific TNFR densities and rate constants for TNF-α–TNFR processes are estimated based on experimental data from our group (31) and other groups as indicated in Table S2 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/.

Values of parameters used to describe TNF-α–induced cell responses, including NF-κB activation and apoptosis (i.e., linking parameters), are estimated via uncertainty analysis by parameter value ranges that are qualitatively consistent with experimental and modeling data on timescales and thresholds for TNF-α–induced cell responses (49, 51, 52).

Using the above methods, we specify a baseline set of parameter values that robustly leads to control of infection in granulomas with organized structures as reported for humans and nonhuman primates (Tables S1, S2, and S5 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/). We then explore parameter changes that shift infection outcome to clearance or uncontrolled growth of M. tuberculosis. To test further the ability of the model to predict different infection outcomes under pathological conditions compatible with both experimental and previous modeling data on granuloma formation, we simulate gene knockouts of previously identified essential components of the M. tuberculosis immune response (e.g., TNF-α, IFN-γ, and T cell knockouts). To do this, we set relevantabilities or rate constants to zero from the beginning of simulations.

Sensitivity analysis

When computational models include parameters describing a large number of known biological processes, it is critical to understand the role that each of these parameters plays in determining output. Sensitivity analysis is a technique to identify critical parameters of a model and quantify how input uncertainty impacts model outputs. Latin hypercube sampling (LHS) is an algorithm that allows multiple parameters to be varied and sampled simultaneously in a computationally efficient manner (53). We use LHS sensitivity analysis as described for application to ABMs (50) to analyze the impact of TNF-α–TNFR trafficking and TNF-α response (linking) parameter values as well as TNF-α–independent and cellular scale parameter values (as listed in Tables S1, S2, and S5 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/) on model outputs. For clarity, these outputs are grouped, as TNF-α function-related outputs (total number of TNF-α–induced events, including NF-κB activation and apoptosis in different types of cells), cellular-level outputs (total bacteria, macrophage, and T cell numbers), tissue-level outputs (granuloma size and average tissue concentrations of TNF-α and chemokines). The correlation of model outputs with each parameter is quantified via calculation of a partial rank correlation coefficient (PRCC). PRCC values vary between −1 (perfect negative correlation) and +1 (perfect positive correlation) and can be differentiated based on p values derived from Student t test. LHS simulations sampled each parameter 250 times. Each sampled parameter set was run four times, and averages of the outputs were used to calculate PRCC values. The choice of the number of simulations is determined by the desired significance level for the PRCC (50, 53). In this study, 250 runs imply that PRCC values above ±0.24 or below −0.24 are significantly different from zero (p < 0.001). To study how processes at different scales interact with each other, we analyze the effect of parameters associated with each scale on the outputs of the same scale (intrascalar sensitivity analysis) as well as on the outputs of the other scale (interscalar sensitivity analysis).

Computer simulations and visualization

The model was implemented in C++. We use Qt, a C++ framework for developing cross-platform applications with a graphical user interface, to visualize and track different aspects of the granuloma, including the structure and molecular concentration gradients, as it forms and is maintained. Simulations can be run with or without graphical visualization. Simulations were run on Linux and Mac operating systems.

Results

Prediction of different infection outcomes at the granuloma level

We first tested whether our multiscale computational model (Fig. 1) could capture key features of granuloma formation and maintenance. Using a combination of parameter estimation and uncertainty analysis as described in Materials and Methods, we identified a set of baseline values for model parameters, including cellular/tissue scale parameters (Table S1 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/), molecular/single-cell scale TNF-α–TNFR parameters (Table S2 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/), and parameters that link the two scales in the model (Table S5 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/). This set of parameter values leads to containment: control of M. tuberculosis infection within a well-circumscribed granuloma containing stable bacterial levels (<10^7 total bacteria) at 200 d postinfection (Fig. 2A, 2B) (see Video 1 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/). This recapitulates a state that has been described as an equilibrium between the host and M. tuberculosis at the level of single granuloma and is referred to as a solid granuloma with caseous center (M. tuberculosis containment) (3, 54). As observed in Video 1 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/, simulated granulomas form as organized immune structures predominately composed of uninfected macrophages surrounding a core of bacteria and infected and activated macrophages with T cells localized at the periphery (4–10). As reported for most animal models of TB, bacterial growth increases logarithmically until reaching a plateau coincident with T cell response initiation (55). As observed in nonhuman primate models as well as in humans, several types of granuloma are observed in M. tuberculosis infection (56). Our multiscale model is also able to recapitulate...
different granuloma types with different abilities to control infection as we vary specific parameters identified as important via sensitivity analysis from their baseline values (see Tables S1, S2, and S5 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/). Cellular scale processes identified to control significantly bacterial numbers, caseation, and granuloma size at 200 d postinfection are bacterial growth, Tg cell-induced STAT1 activation of macrophages, and T cell movement and recruitment (Tγ cells in particular). These results are highlighted in Table I and are consistent with available experimental data reviewed in Refs. 3, 57, and 58 and our previous modeling studies (30, 59). Greater intracellular M. tuberculosis growth rates, in agreement with published data (60), lead to higher bacterial loads and larger granulomas with larger caseation areas. STAT1 activation of macrophages by IFN-γ–producing Tg cells is required for activation of macrophages and killing of intracellular and extracellular M. tuberculosis. Recruitment of IFN-γ–producing Tγ cells to sites of infection is a critical component of immunity to M. tuberculosis as a smaller TNF-α/chemokine concentration threshold for Tγ cell recruitment leads to more effi-

**FIGURE 1.** Schematic representation of the multiscale model of the immune response to M. tuberculosis infection in the lung. A. An overview of selected cell-level ABM rules based on known immunological activities and interactions. B. Schematic representation of binding interactions and reactions controlling TNF-α–TNFR dynamics at the single-cell level with numbers that represent model processes as listed in Table S3 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/.

**FIGURE 2.** Simulation results for the M. tuberculosis dynamics and granuloma structures at 200 d postinfection under different pathological conditions. A. Changes of total number of M. tuberculosis (intracellular and extracellular bacteria, i.e., Bint + Bext) with time for simulation of containment baseline, a scenario of M. tuberculosis clearance, a TNF-α (or TNFRI) knockout scenario, and an IFN-γ knockout scenario, and B–E, Granuloma snapshots for (B) a scenario of containment, (C) clearance of M. tuberculosis infection in less than 5 wk as a result of an efficient immune response, (D) a TNF-α (or TNFRI) knockout scenario, and (E) an IFN-γ knockout scenario. Cell types and status are defined by different colors, as indicated in the upper right corner of the figure. Caseation and vascular sources are also indicated. Bext, extracellular bacteria; Mact, activated macrophage; Mci, chronically infected macrophage; Mi, infected macrophage; Mr, resting macrophage; Tg, proinflammatory IFN-γ-producing T cell; Tc, cytotoxic T cell; Treg, regulatory T cell).
Role of TNFR1 dynamics in mycobacterial granulomas

We know from experimental studies that artificial manipulation of TNF-α concentration via anti–TNF-α treatments negatively affects infection outcome in mice, humans, and nonhuman primates (26, 27, 62, 63). Are there physiological processes within the granuloma that also affect TNF-α concentration, and does alteration of those processes similarly affect infection outcome? To answer this question, we used sensitivity analysis to identify critical TNF-α–independent and cellular scale parameters that influence TNF-α concentration. Notably, processes highlighted in the previous section to be important determinants of bacterial numbers, casation, and granuloma size also significantly impact TNF-α concentration and thus the number of TNF-α–induced NF-κB activation and apoptosis events (30) and a variety of experimental data. We now turn our analysis to the important role that TNF-α plays and the factors that affect the ability of TNF-α to play that role during the immune response to M. tuberculosis.

Cellular scale processes control TNF-α concentration by affecting bacterial load

Table I. Model parameters significantly correlated with outputs of interest, bacterial numbers, granuloma size, casation area, and TNF-α concentration at day 20 postinfection.

<table>
<thead>
<tr>
<th>Selected Model Outputs</th>
<th>Important TNF-α Independent and Cellular Scale Parameters</th>
<th>Important TNF-α–TNFR-Associated Molecular and Linking Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Total number of bacteria</strong></td>
<td>α_{rec} (+)</td>
<td>k_{synthMac} (++)</td>
</tr>
<tr>
<td></td>
<td>P_{STAT} (--)</td>
<td>δ_{TNF} (++)</td>
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<tr>
<td></td>
<td>M_{rec} (++)</td>
<td>δ_{Mac} (++)</td>
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<tr>
<td></td>
<td>T_{move} (--)</td>
<td>k_{Mac} (++)</td>
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<tr>
<td></td>
<td>T_{rec} (--)</td>
<td>δ_{Mac} (++)</td>
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<tr>
<td></td>
<td>T_{refGam} (++)</td>
<td>δ_{Mac} (++)</td>
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<tr>
<td></td>
<td>D_{chem} (++)</td>
<td>k_{Mac} (++)</td>
</tr>
<tr>
<td><strong>Granuloma size</strong></td>
<td>α_{rec} (+)</td>
<td>k_{synthMac} (++)</td>
</tr>
<tr>
<td></td>
<td>P_{STAT} (--)</td>
<td>δ_{TNF} (++)</td>
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<td>M_{rec} (++)</td>
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<td>T_{move} (--)</td>
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<td>δ_{Mac} (++)</td>
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<tr>
<td><strong>Cassation</strong></td>
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<td>k_{synthMac} (++)</td>
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<td>δ_{chem} (++)</td>
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<td></td>
<td>T_{chem} (+)</td>
<td>δ_{Mac} (++)</td>
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<tr>
<td><strong>Average tissue concentration of sTNF</strong></td>
<td>α_{rec} (+)</td>
<td>k_{synthMac} (++)</td>
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<td></td>
<td>P_{STAT} (--)</td>
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<td></td>
<td>T_{chem} (+)</td>
<td>δ_{Mac} (++)</td>
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</table>

*Only parameters with significant PRCC values are indicated. Significant positive and negative correlations are shown using + and − as follows: ++, 0.001 < p < 0.01; +/−, 0.01 < p < 0.05; −/+, p < 0.001.

TNF-α–independent and cellular scale parameter descriptions are as follows: α_{rec}, intracellular M. tuberculosis growth rate; P_{STAT}, probability of STAT-1 activation in Mφ or Mψ; T_{move,Mac}, probability of T cell moving to a macrophage-containing location; T_{rec,Mac}, probability of T cell recruitment; M_{rec,Mac}, probability of Mψ recruitment; T_{ref,Gam,TNF-α/chemokine concentration threshold} for Tψ cell recruitment; P_{apo,Mac}, probability of Fas/FasL apoptosis by Tψ cell; D_{chem}, diffusion coefficient of chemokines; δ_{chem}, chemokine degradation rate constant; T_{chem}, minimum chemokine concentration detection threshold.

**TNF-α–TNFR-Associated parameter descriptions are as follows:** k_{synthMac}, mTNF synthesis rate for macrophages; δ_{opt}, sTNF degradation rate constant; k_{Mac}, equilibrium dissociation constant of sTNF–TNFR1; k_{apo}, TNFR1 internalization rate constant; k_{rec,Mac}, TNFR1 recycling rate constant; T_{ref,Mac}, TNFR1 density on the surface of macrophages; k_{apo,Mac}, rate constant for TNF-α–induced apoptosis in all cell types; k_{opt,Mac}, rate constant for TNF-α–induced NF-κB activation in macrophages; δ_{Mac}, cell surface sTNF–TNFR1 threshold for TNF-α–induced NF-κB activation.

Detailed sensitivity analysis results are presented in Tables S6 and S7 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/.

In contrast, simulations of gene knockouts of essential components of the M. tuberculosis immune response such as TNF-α or TNFR1 knockouts (k_{synthMac} = k_{synthTψMac} = 0 or TNFR1_{mac} = TNFR1_{TψMac} = 0) and IFN-γ knockout (P_{STAT} = 0) lead to uncontrolled growth of M. tuberculosis. This is consistent with a variety of data on the crucial role of these cytokines in immunity to M. tuberculosis (3, 13, 61). In this case, granulomas that form are larger in size, irregular in structure, and include very high numbers of extracellular M. tuberculosis, large numbers of infected macrophages, and widespread casation (dead tissue caused by multiple deaths of macrophages in tissue usually within the core of the granuloma) (Fig. 2A, 2D, 2E) (see Videos 3 and 4 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/). Overall, our multiscale model, which includes molecular (TNF-α–associated), cellular, and tissue scale events, predicts dynamics of M. tuberculosis infection for different infection scenarios, including containment, clearance, and uncontrolled growth of bacteria as well as a variety of structural and functional outcomes that are expected to occur under different pathological conditions. Our results for these conditions are in agreement with our previous study using a model without molecular (TNF-α–associated) events (30) and a variety of experimental data. We now turn our analysis to the important role that TNF-α plays and the factors that affect the ability of TNF-α to play that role during the immune response to M. tuberculosis.

Further, the ability of T cells to migrate through a dense uninfected macrophage network surrounding bacteria and infected macrophages at the core of a granuloma helps determine the efficiency of the T cell-mediated immune response to M. tuberculosis.

In addition to containment, we can reproduce other possible outcomes of M. tuberculosis infection, including clearance and uncontrolled growth of bacteria, by manipulating values of important model parameters. For example, an increase in the ability of T cells to penetrate into the site of infection at the core of granuloma by increasing the value of model parameter T_{move} increases the probability of a T cell moving onto a macrophage-containing microcompartment, significantly increases the efficiency of the T cell-mediated response and thus favors M. tuberculosis clearance (Fig. 2A, 2C) (see Video 2 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/). In contrast, simulations of...
molecular scale and linking parameters associated with TNF-α–TNFR trafficking dynamics balance inflammation and bacterial killing. The effect of changing the rate constant for TNFR1 internalization on sTNF concentration, recruitment of immune cells, macrophage activation, and apoptosis is shown in Fig. 3A. As described above, sTNF-induced TNFR1 internalization, the key process in TNF-α–TNFR trafficking, has a significant impact on responses at molecular, cellular, and tissue scales. The value of the rate constant for TNFR1 internalization \( k_{\text{int1}} \) controls sTNF concentration dynamics during the immune response to \( M. tuberculosis \) (Fig. 3A). The physiological rate of TNFR1 internalization [half-time of \( \sim 15 \text{ min} \) \( (66, 67) \), \( k_{\text{int1}} = 7.7 \times 10^{-5} \text{ s}^{-1} \)] leads to much less extracellular sTNF in the tissue compared with that in the scenario in which sTNF–TNFR1 complex on the cell membrane is not at all \( (k_{\text{int1}} = 0) \) or is very slowly internalized [half-time of \( \sim 115 \text{ min} \), \( k_{\text{int1}} = 1.0 \times 10^{-4} \text{ s}^{-1} \)] (Fig. 3B). Although TNF-α is required for control of \( M. tuberculosis \) infection and the protective granulomatous response, high concentrations of TNF-α may lead to excessive inflammation and cause immunopathology \((61, 68)\). Therefore, we predict that TNF-α–TNFR trafficking plays an important role in preventing excessive inflammation. Indeed, the rate of sTNF-induced internalization of TNFR1 controls the concentration of available TNF-α in tissue and regulates cell infiltration by affecting the extent and dynamics of TNF-α–dependent recruitment and activation of immune cells as well as mediating TNF-α–induced apoptosis (Fig. 3C–F). Thus, a hyperinflammatory state may occur in the absence of a sufficiently rapid sTNF-induced TNFR1 internalization, leading to early and extensive recruitment of macrophages and T cells as well as uncontrolled activation of a large fraction of macrophages that are unable to undergo apoptosis efficiently. Notably, increasing TNFR1 internalization rate constant to \( k_{\text{int1}} = 1.5 \times 10^{-3} \text{ s}^{-1} \) (corresponding with a half-time of \( \sim 7.7 \text{ min} \)) does not have a large effect on either sTNF concentration or immune cell population dynamics but does significantly enhance the number of apoptotic macrophages. However, further analysis reveals that other model outputs may be significantly affected by increasing TNFR1 internalization rate constant.

In addition to an impact on inflammation, TNF-α–TNFR trafficking dynamics are capable of exerting a dramatic effect on the bacterial outcome of \( M. tuberculosis \) infection in a granuloma (Fig. 4). Zero to slow rates of sTNF-induced TNFR1 internalization (half-time of \( \geq 23 \text{ min} \), \( k_{\text{int1}} \leq 5.0 \times 10^{-4} \text{ s}^{-1} \)) favor clearance of bacteria, a moderate (physiological) rate (half-time of \( \sim 15 \text{ min} \), \( k_{\text{int1}} = 7.7 \times 10^{-5} \text{ s}^{-1} \)) leads to containment of bacteria, and a rapid rate of TNFR1 internalization (half-time of \( \sim 7.7 \text{ min} \), \( k_{\text{int1}} = 1.5 \times 10^{-3} \text{ s}^{-1} \)) results in uncontrolled growth of \( M. tuberculosis \) within the 200-d period of infection (Fig. 4) (see Videos 5–8 at http://mathluss.micro.med.umich.edu/lab/movies/Multiscale/GranSim/). However, zero or very slow rates of TNFR1 internalization (e.g., half-time of \( \sim 115 \text{ min} \), \( k_{\text{int1}} = 1.0 \times 10^{-4} \text{ s}^{-1} \)) result in clearance of infection at the expense of extensive inflammation. Thus, our model suggests that there may exist an optimum rate of sTNF-induced TNFR1 internalization that balances the impacts that TNF-α has on control of \( M. tuberculosis \) infection and inflammation in tissue. We now investigate mechanisms underlying this balance.

**Do high rates of TNFR1 internalization and slow rates of TNF-α synthesis have the same effects?**

In the previous section, we showed that the rate of sTNF-induced TNFR1 internalization significantly affects the immune response to \( M. tuberculosis \); a small value of TNFR1 internalization rate constant favors \( M. tuberculosis \) clearance, and increasing the rate of TNFR1 internalization leads to uncontrolled growth of \( M. tuberculosis \). One might argue that such an effect is simply attributable to the role of TNFR1 internalization in reducing sTNF concentration in the granuloma and that therefore an increase or a decrease in the rate of TNF-α synthesis may compensate for the effects of increasing or decreasing the rate of TNFR1 internalization. To test this hypothesis, we compare the effects of manipulating rates of TNFR1 internalization and sTNF synthesis by macrophages on model outputs (such as bacterial numbers and inflammation). As indicated in Fig. 5A, a zero rate of TNFR1 internalization and a high rate of TNF-α synthesis both result in \( M. tuberculosis \) clearance. However, high rates of TNF-α synthesis, in contrast to very slow or zero rates of TNFR1 internalization, do not lead to dramatic increases in sTNF concentration and macrophage activation (Fig. 5B, 5C). This is because impairing TNFR1 internalization has a negative effect on rates of TNF-α–induced apoptosis (Fig. 5D), a process that has been suggested to be important for controlling the level of inflammation.
However, high rates of TNF-α synthesis favor apoptosis of macrophages and thus do not lead to extensive inflammation.

In contrast, a rapid rate of TNFR1 internalization and a small rate of TNF-α synthesis both result in uncontrolled growth of *M. tuberculosis*, although to different extents (Fig. 5A). This difference can be explained by high levels of TNF-α-induced apoptosis in macrophages (and thus infected macrophages) for high values of TNFR1 internalization rate constant, whereas a small rate of TNF-α synthesis leads to lower levels of apoptosis (Fig. 5D).

Apoptosis of infected macrophages can help with reducing intracellular bacterial burden. Thus, our results suggest that the impact of TNF-α–TNFR trafficking on *M. tuberculosis* infection is more complex than simply changing the TNF-α concentration in the granuloma.

**TNFR1 internalization controls the spatial range of TNF-α action within a granuloma**

As demonstrated earlier, sTNF-induced TNFR1 internalization controls both *M. tuberculosis* infection and inflammation in tissue. How does this process play such a key role? We explored the possibility that the spatial range of TNF-α action underlies the important effects of the rate of TNFR1 internalization on granuloma function. By spatial range of TNF-α action, we mean the area surrounding the center of granuloma, as indicated in Fig. 6A, within which macrophages become activated or undergo apoptosis via autocrine or paracrine stimulation pathways (19, 25, 69). As infected macrophages are located in the core of granuloma surrounded by resting macrophages, the spatial range of TNF-α action is correlated with the infection status of macrophages affected by TNF-α. Thus, motivated by our sensitivity analysis (Table S7 at http://malthus.micro.med.umich.edu/lab/movies/Multiscale/GranSim/), we explored the possibility that TNF-α–TNFR trafficking leads to differential effects on TNF-α–mediated responses in cells of different infection status. We analyzed the infection status of macrophages affected by TNF-α–induced events (either NF-κB activation or apoptosis) after *M. tuberculosis* infection by computing infected/resting cell ratios, \(R_{\text{NF-κB}}\) and \(R_{\text{apoptosis}}\), as defined in Materials and Methods (Fig. 6B). These ratios compare TNF-α effects on infected macrophages versus resting macrophages during the *M. tuberculosis* immune response. Our model predicts a very significant effect of TNFR1 internalization on both \(R_{\text{apoptosis}}\) and \(R_{\text{NF-κB}}\) (Fig. 6B). At very slow rates of sTNF-induced TNFR1 internalization (half-time of \(-115\) min, \(k_{\text{int1}} = 1.0 \times 10^{-4} \text{ s}^{-1}\)), resting macrophages are the main cells affected by both TNF-α–mediated apoptosis and NF-κB signaling pathways (\(R_{\text{apoptosis}}\) and \(R_{\text{NF-κB}} < 1\)). However, with a dramatic increase in the rate of TNFR1 internalization (to a half-

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**FIGURE 3.** TNFR1 internalization dynamics control sTNF concentration as well as macrophage and T cell recruitment and behavior. Simulation results show (A) sTNF concentration dynamics, (B) maximum simulated sTNF concentration as a function of TNFR1 internalization rate constant (\(k_{\text{int1}}\)), (C) macrophage recruitment dynamics, (D) maximum fraction of macrophages that become activated after *M. tuberculosis* infection, (E) T cell recruitment dynamics, (F) TNF-α–induced macrophage apoptosis within a 200-d period after *M. tuberculosis* infection. No internalization, \(k_{\text{int1}} = 0\); very slow internalization, \(k_{\text{int1}} = 1.0 \times 10^{-4} \text{ s}^{-1}\); slow internalization, \(k_{\text{int1}} = 5.0 \times 10^{-4} \text{ s}^{-1}\); moderate internalization, \(k_{\text{int1}} = 7.7 \times 10^{-4} \text{ s}^{-1}\); and rapid internalization, \(k_{\text{int1}} = 1.5 \times 10^{-3} \text{ s}^{-1}\).
Infection for moderate \((k)\) \(R\) on type and status in granuloma snapshots are the same as those shown and defined in Fig. 2. Time of \(M.\) \(tuberculosis\) \(a\) become the main responders to TNF- \(a\) important TNF- \(a\) other processes. We analyzed the effect of varying values of im-

 significance correlation was observed between bacterial levels and \(R\) and \(R\) and \(\sim\) time of \(M.\) \(tuberculosis\) \(a\) portons TNF- \(a\) dynamics within a 200-d period after \(M.\) \(tuberculosis\) infection. While a significant fraction of resting macrophages sur-

 Fig. 4. TNFR1 internalization dynamics control bacterial load during \(M.\) \(tuberculosis\) infection. Simulation results show (A) \(M.\) \(tuberculosis\) dynamics within a 200-d period after \(M.\) \(tuberculosis\) infection, (B) granuloma outcomes and bacterial load 200 d postinfection, (C) granuloma snapshot at the time of \(M.\) \(tuberculosis\) clearance (day 45) in the absence of TNFR1 internalization \(k_{\text{int}} = 0\), (D, E) granuloma snapshots 200 d after \(M.\) \(tuberculosis\) infection for moderate \(k_{\text{int}} = 7.7 \times 10^{-3} \text{ s}^{-1}\) and rapid \(k_{\text{int}} = 1.5 \times 10^{-3} \text{ s}^{-1}\) rates of TNFR1 internalization. The colors representing cells of different type and status in granuloma snapshots are the same as those shown and defined in Fig. 2.

Fig. 7, an increase of one order of magnitude in cell surface sTNF–TNFR1 concentration threshold for NF-\(\kappa\)B activation and TNF-\(\alpha\) degradation rate constant or a decrease of one order of magnitude in NF-\(\kappa\)B activation rate constant and the rate of mTNF synthesis by macrophages around baseline parameter values led to significant increases in both \(R_{\text{apoptosis}}\) and \(R_{\text{NF-\kappa B}}\) as well as bacterial levels. Outcomes of uncontrolled growth of \(M.\) \(tuberculosis\) generally occur at \(R_{\text{apoptosis}}\) and \(R_{\text{NF-\kappa B}}\) values of 1–10 or greater, and the chance of achieving clearance is greater for smaller values of these ratios. However, as indicated in Fig. 7E, when macrophage TNFR1 density is varied, the correlation between these ratios and bacterial levels (in clearance and containment cases in particular) does not appear very significant. This is probably because TNFR1 density has contradictory effects on TNF-\(\alpha\) functions; although greater TNFR1 densities lead to more sensitive responses to smaller TNF-\(\alpha\) concentrations, at the same time such larger densities enhance TNF-\(\alpha\) uptake by macrophages limiting TNF-\(\alpha\) availability in a granuloma. Overall, we suggest that infected/resting cell ratios we introduced in this study to compare TNF-\(\alpha\) effects on infected versus resting macrophages, \(R_{\text{apoptosis}}\) and \(R_{\text{NF-\kappa B}}\), translate the effects of a variety of TNF-\(\alpha\)-associated processes to granuloma outcomes.

Discussion

TNF-\(\alpha\) was long suggested, based on experimental data from mice, to be essential for formation of granulomas in response to \(M.\) \(tuberculosis\) (17, 26, 70). However, recent TNFR1 knockout and TNF-\(\alpha\) neutralization experiments in zebrafish and nonhuman primate models have shown that TNF-\(\alpha\), although not required for

A robust metric for assessing TNF-\(\alpha\) impact on granuloma function

In the previous section, we demonstrated that the impact of the rate of TNFR1 internalization on bacterial levels in a granuloma is sig-

Fig. 6C–F displays how granulomas are affected by the rate at which sTNF–TNFR1 complexes become internalized; these snapshots are taken early after T cell recruitment to the site of infection. While a significant fraction of resting macrophages sur-

around the infected core of granuloma become activated as a result of slow rates of TNFR1 internalization (i.e., there is a greater spatial range of TNF-\(\alpha\) action, as seen in Fig. 6C), only a small number of infected macrophages in the core may become activated with a rapid rate of TNFR1 internalization (Fig. 6F). Thus, we suggest that the spatial range of TNF-\(\alpha\) action within a granuloma is an important factor that controls the effect of TNFR1 internalization on the bacterial outcome of \(M.\) \(tuberculosis\) infection as well as the level of inflammation in the tissue.

the rate of TNFR1 internalization dynamics control bacterial load during \(M.\) \(tuberculosis\) infection. Simulation results show (A) \(M.\) \(tuberculosis\) dynamics within a 200-d period after \(M.\) \(tuberculosis\) infection, (B) granuloma outcomes and bacterial load 200 d postinfection, (C) granuloma snapshot at the time of \(M.\) \(tuberculosis\) clearance (day 45) in the absence of TNFR1 internalization \(k_{\text{int}} = 0\), (D, E) granuloma snapshots 200 d after \(M.\) \(tuberculosis\) infection for moderate \(k_{\text{int}} = 7.7 \times 10^{-3} \text{ s}^{-1}\) and rapid \(k_{\text{int}} = 1.5 \times 10^{-3} \text{ s}^{-1}\) rates of TNFR1 internalization. The colors representing cells of different type and status in granuloma snapshots are the same as those shown and defined in Fig. 2.

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Discussion

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the formation of a granuloma, is important to restrict mycobacterial growth in a granuloma (27, 71). This suggests that TNF-α activities within a granuloma determine our ability to control M. tuberculosis infection. The important questions are, then, how TNF-α activities influence granuloma function, and what mechanisms control TNF-α activities in a granuloma during a long-term immune response to M. tuberculosis? To answer these questions, we need information about the spatial and temporal dynamics of TNF-α concentration during granuloma development in vivo. These experiments are not at present feasible, and thus these questions have remained unanswered. In this study, we use computational modeling/systems biology to address these questions. Our novel hypothesis is that events at different biological scales (molecular, cellular, and tissue scales) may influence TNF-
α activities in a granuloma, ultimately determining a granuloma’s ability to control infection and inflammation. To address this hypothesis, our model was developed to link the dynamics of molecular scale TNF-α–TNFR interactions that occur on the second to minute timescales to cellular/tissue scale events that control the long-term immune response to M. tuberculosis. One of our interesting findings is that both TNF-α–independent cellular/tissue scale events (e.g., T cell recruitment or chemotactic movement of immune cells) and TNF-α–associated molecular scale processes (e.g., mTNF synthesis or TNFR1 internalization) influence TNF-α availability and activity in the granuloma, but in different ways. TNF-α–independent cellular scale processes influence bacterial numbers, and that controls TNF-α availability. However, TNF-α–associated molecular scale processes directly affect TNF-α availability and activities that control both the level of inflammation and bacterial numbers. Thus, there is an interplay between TNF-α availability and bacterial population at the site of infection that is controlled by the combined effects of molecular and cellular scale processes. An equilibrium state in this interplay leads to control of infection within a granuloma.

Our model reveals for the first time, to our knowledge, the importance of TNF-α–associated molecular processes (TNFR1 internalization in particular) in immunity to M. tuberculosis. We found that TNFR1 internalization regulates a balance between paracrine and autocrine TNF-α–induced responses, including NF-κB activation and apoptosis, in resting versus infected macrophages. Because resting macrophages do not express TNF, they become activated by TNF-α–producing cells only in a paracrine manner. However, infected macrophages express and release TNF-α to the extracellular space. Hence, they can become activated under the effect of TNF-α via both autocrine and paracrine pathways. Our results show that TNFR1 internalization favors activation of infected macrophages in an autocrine manner by restricting the diffusion of TNF-α from TNF-α–producing cells. TNF-α–induced activation of resting macrophages in addition to infected macrophages is necessary for controlling M. tuberculosis infection. Uncontrolled activation of resting macrophages, in contrast, may result in excessive inflammation. Thus, a balance between the autocrine and paracrine TNF-α–induced responses is required for an efficient granuloma response to M. tuberculosis, and an optimum rate of TNFR1 internalization can provide this balance. This finding can be considered in future studies examining approaches to control and therapy of TB or inhibition of TB reactivation, as several ways have already been proposed to influence the rate of TNFR1 internalization in vitro (42, 72, 73).

Another novel hypothesis from this study is that the efficacy of TNF-α in controlling M. tuberculosis infection is strongly affected by whether macrophages induced by TNF-α–mediated signaling pathways (NF-κB activation and apoptosis) are infected. Bacterial numbers are positively correlated with the ratio of infected

**FIGURE 7.** The impact of processes associated with TNF-α–TNFR on granuloma outcome is correlated with infection status of macrophages that undergo TNF-α–mediated apoptosis or NF-κB activation. Simulation results show the effect of (A) cell surface sTNF–TNFR1 concentration threshold for NF-κB activation (τ_{NF-κB}), (B) sTNF degradation rate constant (δTNF), (C) NF-κB activation rate constant (k_{NF-κB}), (D) rate of mTNF synthesis by macrophages (k_{synthMac}), and (E) macrophage TNFR1 density (TNFR1_{mac}) on infected/resting cell ratios R_{apoptosis} and R_{NF-κB} within a 200-d period after M. tuberculosis infection. Also indicated is granuloma outcome (clearance, containment, or uncontrolled growth of M. tuberculosis).
macrophages to (uninfected) resting macrophages that become activated by TNF-α. Thus, we suggest that this ratio is a critical factor that controls the outcome of *M. tuberculosis* infection at the granuloma level. This might be of particular interest in the case of TB reactivation as a result of using TNF-α-neutralizing drugs (e.g., for treatment of inflammatory diseases such as rheumatoid arthritis and Crohn’s disease). As drug penetrates into a granuloma, resting macrophages, compared with infected macrophages in the granuloma core, are exposed to smaller concentrations of TNF-α and are affected by higher concentrations of the drug. This can potentially impair TNF-α function, leading to TB reactivation.

Finally, our findings may predict new therapies for control of TB as they suggest novel host targets (e.g., TNFR1 internalization and NF-κB activation) that play key roles in control of *M. tuberculosis* immune response. Further modeling studies including molecular detail of additional processes, such as those involving other cytokines (e.g., IL-10, IL-6, and IL-12) and chemokines, and using a similar approach to that identified in this study may also identify other important targets for therapy. Our multiscale computational model also provides a platform at the level of single granuloma to identify and compare therapeutic strategies as well as to investigate mechanisms by which TNF-α-neutralizing drugs (used to treat inflammatory diseases) or other drugs that diffuse in TB lesions may interfere with immune response to *M. tuberculosis* and reactivating TB.

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